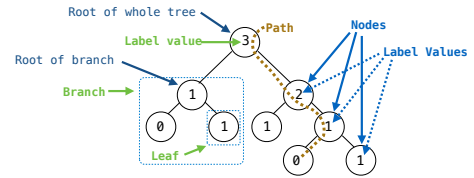


61A Lecture 19

Announcements

Tree Class

Tree Review



Recursive description (wooden trees):

A tree has a label value and a list of branches
Each branch is a tree
A tree with zero branches is called a leaf

Relative description (family trees):

Each location in a tree is called a node
Each node has a value
One node can be the parent/child of another
Top node of tree is its root

Tree Class

A Tree has a label value and a list of branches; each branch is a Tree

```
class Tree:
    def __init__(self, label, branches=[]):
        self.label = label
        for branch in branches:
            assert isinstance(branch, Tree)
        self.branches = list(branches)

def fib_tree(n):
    if n == 0 or n == 1:
        return Tree(n)
    else:
        left = fib_tree(n-2)
        right = fib_tree(n-1)
        fib_n = left.label + right.label
        return Tree(fib_n, [left, right])

def tree(label, branches=[]):
    for branch in branches:
        assert is_tree(branch)
    return [label] + list(branches)

def label(tree):
    return tree[0]

def fib_tree(n):
    if n == 0 or n == 1:
        return tree(n)
    else:
        left = fib_tree(n-2)
        right = fib_tree(n-1)
        fib_n = label(left) + label(right)
        return tree(fib_n, [left, right])
```

(Demo)

Side Excursion: Equality

If x and y are two objects, the equality test, $x == y$, does not automatically mean what you want it to mean.

For example, `Tree(4) != Tree(4)` but after performing `x = Tree(4)`, we do have `x == x`

The reason for this is that in Python,

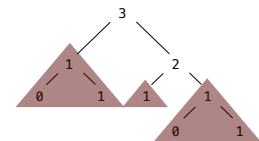
- All values (conceptually, at least) are in fact pointers to objects, and
- By default, `==` on pointers compares the pointers themselves ("are these pointing at exactly the same object?").
- That is, by default `==` and `!=` are the same as the `is` and `is not` operators.
- That can be changed on a class-by-class basis. For example, `==` on numbers, lists, tuples, strings, sets, and dictionaries means what we expect: the contents are the same.

Tree Mutation

Example: Pruning Trees

Removing subtrees from a tree is called pruning

Prune branches before recursive processing



```
def prune(t, n):
    """Prune sub-trees whose label value is n."""
    t.branches = [b for b in t.branches if b.label != n]
    for b in t.branches:
        prune(b, n)
```

(Demo)

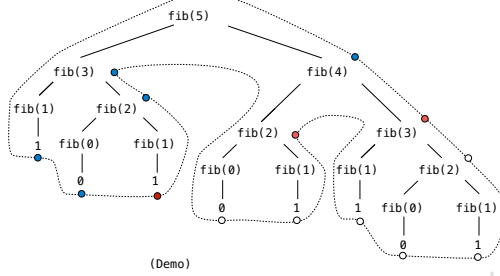
Example: Pruning Trees

Removing subtrees from a tree is called *pruning*

Prune branches before recursive processing

E.g., want to prune cached (previously memorized) values.

- Memoization:**
- Returned by fib
 - Found in cache
 - Skipped



(Demo)

Hailstone Trees

Hailstone Trees

Pick a positive integer n as the start

If n is even, divide it by 2

If n is odd, multiply it by 3 and add 1

Continue this process until n is 1

(Demo)

```
def hailstone_tree(k, n=1):  
    """Return a Tree in which the paths from the  
    leaves to the root are all possible hailstone  
    sequences of length k ending in n."""
```

All possible n that start a
length-8 hailstone sequence

(Demo)

