Instructions

Form a small group. Start on the first problem. Check off with a helper or discuss your *solution process* with another group once everyone understands *how to solve* the first problem and then repeat for the second problem . . .

You may not move to the next problem until you check off or discuss with another group and everyone understands why the solution is what it is. You may use any course resources at your disposal: the purpose of this review session is to have everyone learning together as a group.

1 Scheme

1.1 What would Scheme display?

```
(a) > '(1 2 3)

(b) > '(1 . (2 . (3 . ())))

(c) > '(((1 . 2) . 3) 4 . (5 . 6))

(d) > (cons 1 2)

(e) > (cons 2 '())

(f) > (cons 1 (cons 2 '()))

(g) > (cons 1 (cons 2 3))

(h) > (cons (cons (car '(1 2 3)) (list 2 3 4)) (cons 2 3))

(i) > (car (cdr (car '((1 2) 3 (4 5)))))
```

(j) > (cddr'((1 2) 3 (4 5)))

1.2 Define sixty-ones. Return the number of times that 1 follows 6 in the list.

```
> (sixty-ones '(4 6 1 6 0 1))
1
> (sixty-ones '(1 6 1 4 6 1 6 0 1))
2
> (sixty-ones '(6 1 6 1 4 6 1 6 0 1))
3
```

1.3 Identify the bug(s) in this program.

3

```
> (add-to-all 'foo '((1 2) (3 4) (5 6)))
((foo 1 2) (foo 3 4) (foo 5 6))
```

(b) Rewrite add-to-all tail-recursively.

1.5 Define sublists. Hint: use add-to-all.

```
> (sublists '(1 2 3))
(() (3) (2) (2 3) (1) (1 3) (1 2) (1 2 3))
```

1.6 (a) Define reverse. Hint: use append.

(b) Define reverse tail-recursively. Hint: use a helper function and cons.

Interpreters

 $^{2.1}$ Circle the number of calls to $scheme_eval$ and $scheme_apply$ for the code below.

```
(a) scm> (+12)
    3
     scheme_eval
                  1 3
     (b) scm> (if 1 (+ 2 3) (/ 1 0))
    5
     scheme_eval
                  1
                     3
     (c) scm> (or #f (and (+ 1 2) 'apple) (- 5 2))
    apple
     scheme_eval
                  6 8
                           10
                  1 2 3
     scheme_apply
                            4
 (d) scm> (define (add x y) (+ x y))
    add
    scm> (add (- 5 3) (or 0 2))
     scheme_eval
                  12
                      13
                          14
                              15
                       2
     scheme_apply
                   1
                           3
                               4
Identify the number of calls to scheme_eval and scheme_apply.
 (a) scm> (define pi 3.14)
    рi
    scm> (define (hack x)
```

```
(cond
                 ((= x pi) pwned)
                 ((< x 0) (hack pi))
                 (else (hack (-x 1))))
   hack
(b) scm> (hack 3.14)
   pwned
(c) scm> ((lambda (x) (hack x)) \emptyset)
   pwned
```

3 Streams

3.1 Implement merge, which takes two streams \$1 and \$2 whose elements are ordered.

merge returns a stream that contains elements from \$1 and \$2 in sorted order, eliminating repetition. You may assume \$0 and \$1 themselves do not contain repeats.

\$1 and \$2 may or may not be infinite streams.

```
(define (merge s0 s1)
(cond ((null? s0) s1)
((null? s1) s0)
```

```
)
```

A famous problem, first raised by Richard Hamming, is to enumerate, in ascending order with no repetitions, all positive integers with no prime factors other than 2, 3, or 5. These are called regular numbers. One obvious way to do this is to simply test each integer in turn to see whether it has any factors other than 2, 3, and 5. But this is very inefficient, since, as the integers get larger, fewer and fewer of them fit the requirement.

As an alternative, we can write a function that returns an infinite stream of such numbers. Let us call the stream of numbers **s** and notice the following facts about it.

- s begins with 1.
- The elements of (scale-stream s 2) are also elements of s.
- The same is true for (scale-stream s 3) and (scale-streams5).
- These are all of the elements of s.

Now all we have to do is combine elements from these sources. Use the merge function you defined previously to fill in the definition of make-s:

```
(define (make-s)
```

)

4 Iterators

4.1 Define a generator that yields the sequence of perfect squares. The sequence of perfect squares looks like: 1, 4, 9, 16...

```
def perfect_squares():
```

4.2 Implement zip, which yields a series of lists, each containing the nth items of each iterable. It should stop when the smallest iterable runs out of elements.

4.3 Implement generate_subsets that returns all subsets of the positive integers from 1 to n. Each call to this generator's next method will return a list of subsets of the set $\{1, 2, ..., n\}$, where n is the number of previous calls to next.

5 SQL

pizzas defines the name, open, and close hours of pizzarias. meals defines typical meal times. A pizzaria is open for a meal if the meal time is within open and close.

```
create table pizzas as
  select "Pizzahhh" as name, 12 as open, 15 as close union
  select "La Val's"
                            , 11
                                         , 22
                                                        union
  select "Sliver"
                                                        union
                             , 11
                                           20
  select "Cheeseboard"
                                         , 23
                             , 16
                                                        union
  select "Emilia's"
                             , 13
                                         , 18;
create table meals as
  select "breakfast" as meal, 11 as time union
  select "lunch"
                              , 13
                                           union
  select "dinner"
                              , 19
                                           union
  select "snack"
                              , 22;
```

5.1 There's nothing wrong with going to the same pizza place for meals greater than 6 hours apart, right? Create a table double with the earlier meal, the later meal, and the name of the pizza place. Only include rows that describe two meals that are more than 6 hours apart and a pizza place that is open for both of the meals.

create table double as

```
> select * from double where name="Sliver";
breakfast|dinner|Sliver
```

5.2 For each meal, list all the pizza options. Create a table options that has one row for every meal and three columns. The first column is the meal, the second is the total number of pizza places open for that meal, and the last column is a commaseparated list of open pizza places in alphabetical order. Assume that there is at least one pizza place open for every meal. Order the resulting rows by meal time.

Hint: Define a recursive table in a with statement that includes all partial lists of options, then use the **max** aggregate function to pick the full list for each meal.

create table options as

```
> select * from options where meal="dinner";
dinner|3|Cheeseboard, La Val's, Sliver
```